

Trapezium Rule-2

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Select TABLE mode from the main menu by using the arrow keys to highlight the TABLE icon or pressing 7.



Note:
$$\text{Area} = \frac{1}{2}h[y_0 + 2y_1 + 2y_2 + \dots + 2y_{n-1} + y_n]$$
 Where
$$h = \frac{x_n - x_0}{n}$$

Also known as the trapezoidal rule

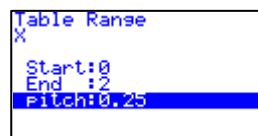
You can remember what is inside the $[y_0 + 2y_1 + 2y_2 + \dots + 2y_{n-1} + y_n]$ by the sequence: **1 2 2 2 2 2 2 2 2 1**

Example: Calculate the area bounded by the x-axis and the curve $y = x.e^x$ between $x = 0$ and $x = 2$, in steps of 0.25.

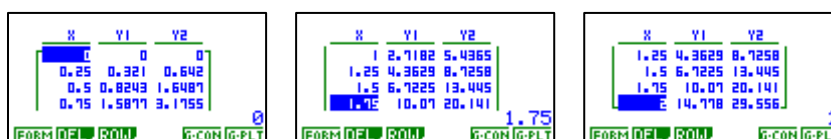
Answer: Enter **TABLE** mode and enter in the Function:
 $x.e^x$ in the Y1 space and
 $2(x.e^x)$ in the Y2 space.



Select **F5 RANGE** to enter $x = 0$, the **Start** value and $x = 2$, the **End** value and **pitch** to .25, being the step length.
 Then **EXIT**.



To create the table of values, x, Y1 and Y2 press the **F6** key



Reading off the required values from Y1:

$$\begin{aligned} \text{Area} &= \frac{1}{2} \times .25 \times [0 + 2 \times 0.321 + 2 \times 0.824 + 2 \times 1.588 + 2 \times 2.718 + 2 \times 4.363 + \\ &\quad 2 \times 6.723 + 2 \times 10.07 + 14.778] \\ &= 0.125 \times [0 + 0.642 + 1.648 + 3.176 + 5.436 + 8.726 + 13.446 + 20.14 + 14.778] \\ &= 0.125 \times 69.992 \\ &= 8.499 \text{ sq units} \end{aligned}$$

OR reading off the required values from Y1 and Y2:

$$\begin{aligned} \text{Area} &= \frac{1}{2} \times 0.25 \times [0 + 0.642 + 1.648 + 3.176 + 5.436 + 8.726 + 13.446 + 20.14 + 14.778] \\ &= 0.125 \times 69.992 \\ &= 8.499 \text{ sq units} \end{aligned}$$